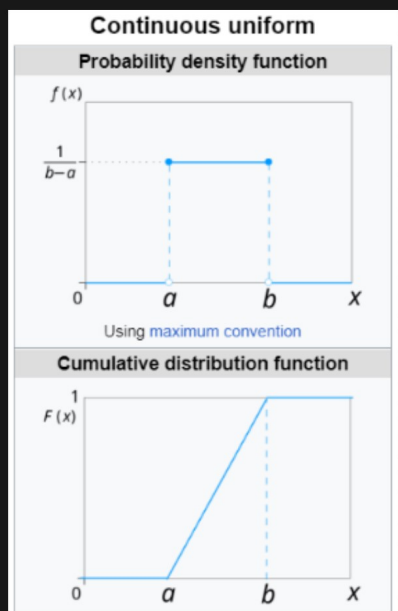


Uniform Distribution

- ① Continuous Uniform Distribution (pdf)
- ② Discrete Uniform Distribution (pmf)

① Continuous Uniform Distribution [Continuous Random Variable]

In probability theory and statistics, the continuous uniform distributions or rectangular distributions are a family of symmetric probability distributions. Such a distribution describes an experiment where there is an arbitrary outcome that lies between certain bounds. The bounds are defined by the parameters, a and b which are the minimum and maximum values.



Notation : $U(a,b)$

Parameters : $-\infty < a < b < \infty$

$$Pdf = \begin{cases} \frac{1}{b-a} & x \in [a,b] \\ 0 & \text{otherwise} \end{cases}$$

$$cdf = \begin{cases} 0 & \text{for } x < a \\ \frac{x-a}{b-a} & \text{for } x \in [a,b] \\ 1 & \text{for } x > b \end{cases}$$

$$\text{Mean} = \frac{1}{2}(a+b) //$$

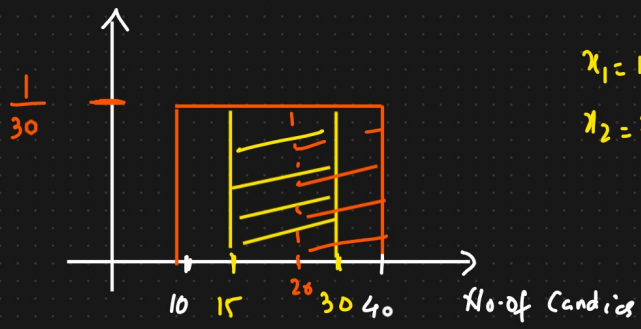
$$\text{Median} = \frac{1}{2}(a+b) //$$

$$\text{Variance} = \frac{1}{12}(b-a)^2 =$$

Eg: The number of candies sold daily at a shop is uniformly distributed with a maximum of 40 candies and a minimum of 10

i) Probability of daily sales to fall between 15 and 30?

Ans)



$$Pr(15 \leq X \leq 30) = (x_2 - x_1) * \frac{1}{b-a}$$

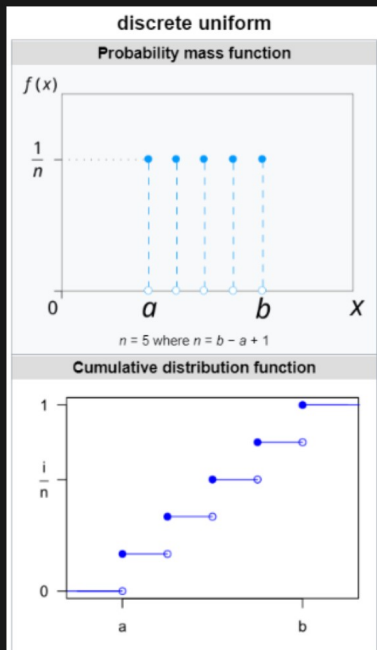
$$= (30 - 15) * \frac{1}{30}$$

$$= 0.5 //$$

$$Pr(X > 20) = (40 - 20) * \frac{1}{30} = 0.66 = 66\%$$

② Discrete Uniform Distribution

In probability theory and statistics, the discrete uniform distribution is a symmetric probability distribution wherein a finite number of values are equally likely to be observed; every one of n values has equal probability $1/n$. Another way of saying "discrete uniform distribution" would be "a known, finite number of outcomes equally likely to happen".



① Discrete Random Variable

② pmf

Eg: Rolling a dice \Rightarrow Fair dice $\{1, 2, 3, 4, 5, 6\}$

$$Pr(1) = 1/6$$

$$Pr(2) = 1/6$$

$$Pr(3) = 1/6$$

$$\vdots = 1/6$$

$$1/n \Rightarrow n = b - a + 1 = 6 - 1 + 1 = 6$$

$1/6$

Notation $U(a, b)$

Parameters a, b where $b \geq a$

PMF $1/n$

Mean $\sim \frac{a+b}{2}$
Median $\sim \frac{a+b}{2}$